

# Optimizing Neural Networks with Multi-Objective Bayesian Optimization and Augmented Random Search

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## Motivation

### Problem

- To enable DNN deployment at the edge, there are often tight resource constraints that can be met by network pruning, weight quantization, and other graph-based and algorithmic optimizations<sup>1</sup> that can be controlled by hyperparameters.
- However, optimizing the assignment of values to these hyperparameters, i.e., solving a multi-objective optimization problem, is expensive because the DNN training and compression pipeline must be executed once for each possible combination of parameters.

### Goal

- Use Multi-Objective Bayesian Optimization<sup>2</sup> (MoBOpt) to enable optimized DNN deployment with a limited search budget.
- Investigate and improve MoBOpt strategies such as ParEGO<sup>3</sup>, for which we observed that in some situations they fail to reliably find the global optimum.

### Contribution

- We propose to use an ensemble of competing local Reinforcement Learning (RL) agents, which we train on different parts of the surrogate model using Augmented Random Search<sup>4</sup> (ARS) to more effectively exploit their encoded knowledge of the target space.
- We show experimentally that we can improve on several existing MoBOpt and evolutionary strategies for two different datasets and DNN architectures.

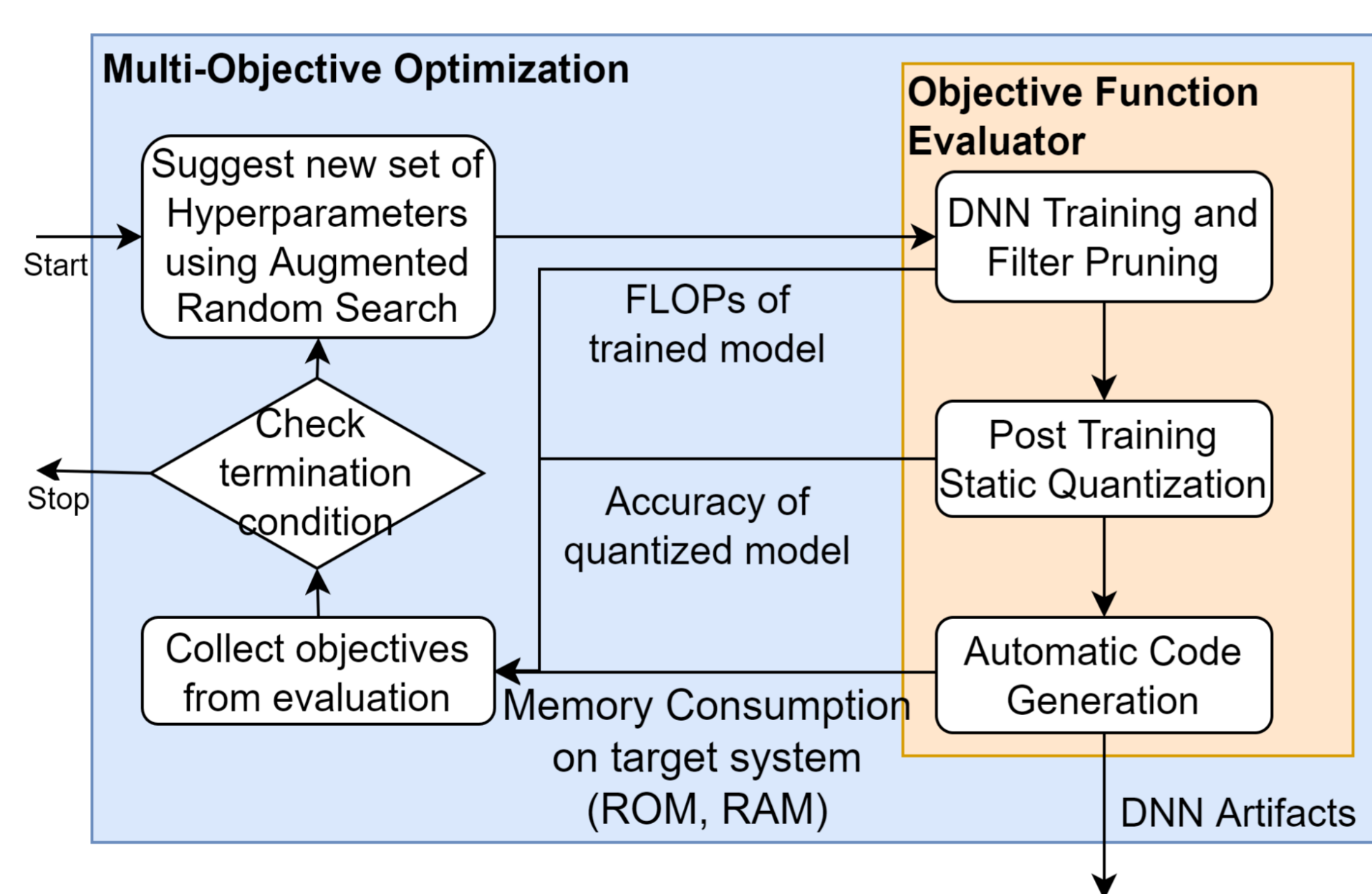


Figure 1. Overview of our RL-based multi-objective Bayesian DNN optimization approach.

## Method

- Perform optimization of the objective function  $f(x) = [f_1(x), \dots, f_n(x)]$  by sampling sets of hyperparameters until the search budget is exhausted.
- For each sample, perform a nested optimization on the Bayesian surrogate model fitted by maximising the marginal likelihood of previous evaluations of  $f(x)$ . Use a Latin hypercube during the first samples to obtain an initial prior.
- Train each competing local MLP RL policy  $\pi_l$  on different parts of the search space using the centers of  $l$ -means clusters of the Pareto-front as starting points. For each training step  $i \dots$

- Sample directions  $\varphi_1, \varphi_2, \dots, \varphi_N \in \mathbb{R}^{n \times m}$  with i.i.d. standard normal entries.
- Perform  $j \in \{1, 2, \dots, N\}$  rollouts over the horizon  $H$  from the GP using

$$\pi_{l,j,+}(x) = (\theta_l + v\varphi_j)$$

$$\pi_{l,j,-}(x) = (\theta_l - v\varphi_j)$$

- Collect rewards  $r(\pi_{l,j,+}(x))$  and  $r(\pi_{l,j,-}(x))$  by scaling objectives to a single one using Chebyshev scalarization<sup>3</sup> and compute the Expected Improvement<sup>2</sup> (EI).
- Evaluate EI empirically using Monte Carlo Sampling and the reparametrization trick<sup>5</sup>
- Sort the  $N$  directions by  $\max\{r(\pi_{l,j,+}(x)), r(\pi_{l,j,-}(x))\}$  and then update the MLP weights using a top- $K$  selection.

$$\theta_{l,i+1} = \theta_{l,i} + \frac{\alpha}{K\sigma_R} \sum_{k=1}^K (r(\pi_{l,j,+}(x)) - r(\pi_{l,j,-}(x))) \varphi_k$$

where  $\sigma_R$  is the standard deviation of the reward used in the update step

- Validate trained policies  $\pi_i$  and suggest hyperparameters proposed by the best performing policy to be evaluated next by the function evaluators (outer optimization loop).

## Experiments

### Experiment 1: ResNet18, CIFAR10

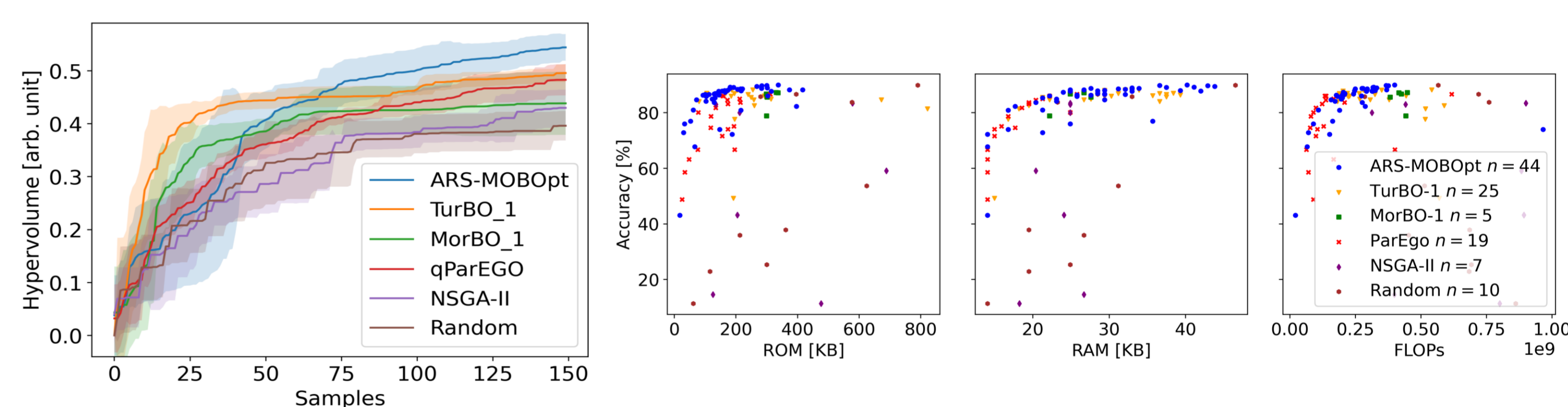


Figure 2. Hypervolume and feasible Pareto fronts of optimizations performed for two problems (ResNet18, CIFAR10 and MobileNetV3, DaLiAc) with a search budget of 150 samples and 5 seeds each.

### Experiment 2: Synthetic Problem

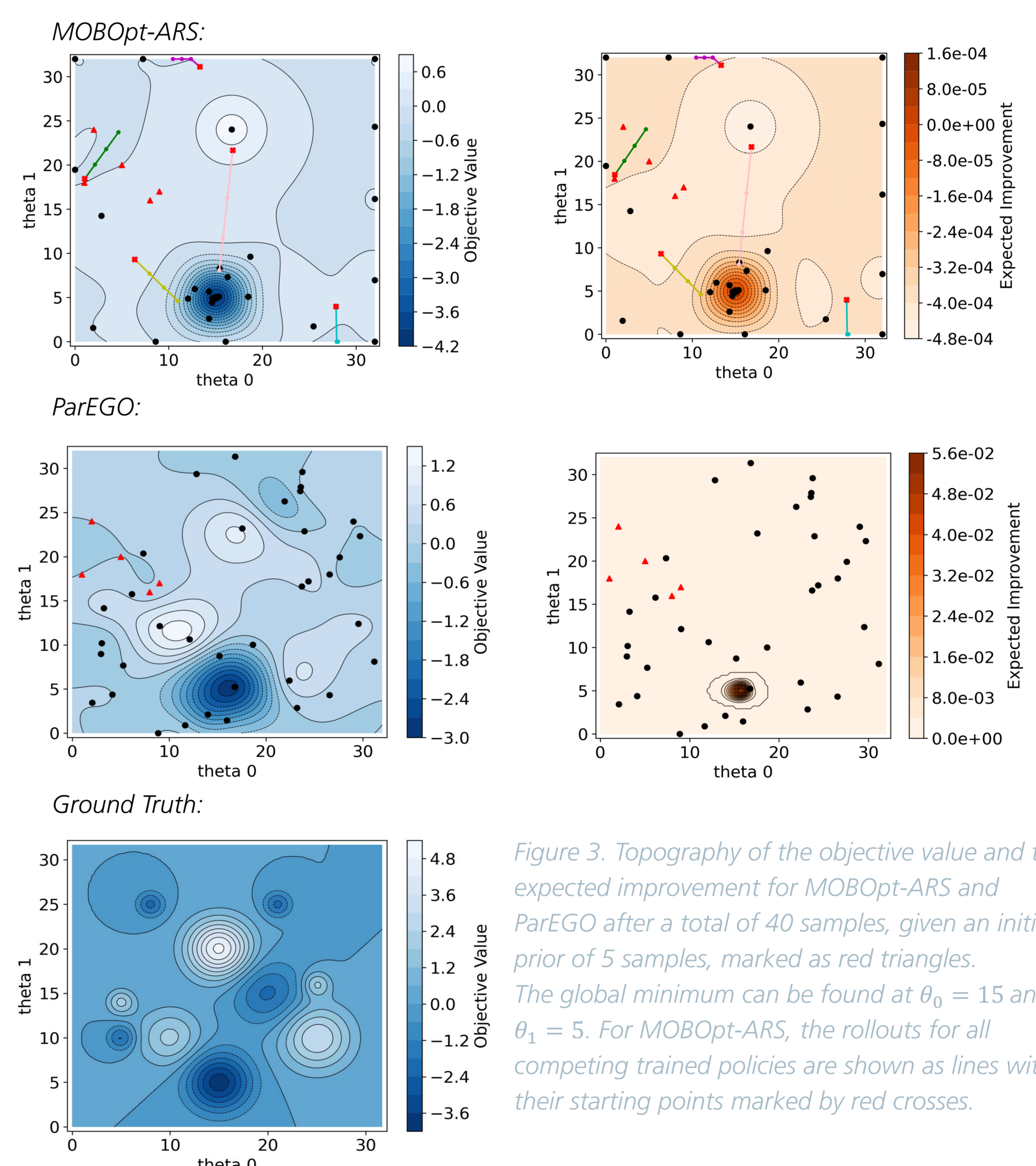


Figure 3. Topography of the objective value and the expected improvement for MOBOpt-ARS and ParEGO after a total of 40 samples, given an initial prior of 5 samples, marked as red triangles. The global minimum can be found at  $\theta_0 = 15$  and  $\theta_1 = 5$ . For MOBOpt-ARS, the rollouts for all competing trained policies are shown as lines with their starting points marked by red crosses.

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